

Wave energy in the Mediterranean

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Theoretical background

Evaluation of wave energy flux for real sea states

- Real sea states are not composed of deterministic simple harmonic waves
- Different propagation directions, lengths and frequencies
- Stochasticity should be also included

According to Pierson and Longuet-Higgins model, the sea surface elevation is described as a stationary, ergodic and Gaussian stochastic process

$$\eta(t;\beta)=\sum_{i=1}^NA_i\cos(\omega_it+\phi_i(\beta)),$$

where $\eta(t;\beta)$ denotes the sea surface elevation, A_i , ω_i , and ϕ_i are the amplitude, frequency and phase of the harmonic component i , respectively. ϕ is a random variable uniformly distributed in $[0,2\pi]$. Sea state parameters can be derived by using the wave power spectral density function $S(f)$, where f is the frequency.

Use is made of specific spectral parameters, such as: the significant wave height H_S , the mean energy period T_e , the spectral peak wave period T_p . The wave power per unit wave-crest length for a real sea state is estimated as follows:

$$P=\frac{\rho g^2}{64\pi}H_S^2T_e,$$

where ρ is the sea water density (1025 kg/m³) and the significant wave height and the energy period are defined through the zeroth and negative first – order spectral moments, i.e.:

$$H_S=4\sqrt{m_0},\quad T_e=\frac{m_0}{m_{-1}},$$

where

$$m_n=\int_0^{2\pi}\int_0^\infty f^nS(f,\theta)dfd\theta,\quad n=\cdots,-1,0,1,2\ldots$$

Wave Data

Wave reanalysis data

- Med – WAV, Copernicus Marine Service
- 1993 – 2020, with a temporal resolution 1-h
- Spatial resolution 1/24° x 1/24° ~3.65 km

In – situ wave measurements

- Greek Seas: POSEIDON marine monitoring network (3-h)
- Spanish Seas: Spanish Port Authority (1-h)

Evaluation of the reanalysis wave data

Collocate the reanalysis dataset with the buoy data in space and time based on the four nearest grid points, applying the inverse distance weighting interpolation function:

$$H_{SR}=\frac{\sum_{i=1}^4\frac{H_{S_{Ri}}}{d_i^2}}{\sum_{i=1}^4\frac{1}{d_i^2}},\quad i=1,2,3,4,$$

where, $H_{S_{Ri}}$, $i=1,2,3,4$ is the significant wave height in the 4 nearest (to the buoy location) grid points and d_i , $i=1,2,3,4$, are the corresponding distances from the buoy location.

- Compare the significant wave heights H_{SR} from reanalysis dataset and H_{SB} from the buoys
- Evaluation parameters : mean relative absolute error (*MRAE*), mean absolute error (*MAE*), *Bias*, root mean square error (*RMSE*) and Pearson correlation coefficient (ρ).

Numerical results

Evaluation of the reanalysis dataset

Greek Seas

- Best performance of the model in Pylos: *MRAE* =0.180, *MAE*=0.168 m, *bias*=0.080 m, *RMSE*=0.237 m, $\rho=0.959$
- Good performance in Athos: *MRAE* (0.290), *MAE* (0.170 m), *bias* (0.064 m), *RMSE* (0.239 m), correlation coefficient (0.953).
- Lower performance in Santorini: *MRAE* (0.290), *MAE* (0.231 m), *bias* (0.161 m), *RMSE* (0.3189 m), correlation coefficient (0.913).

Spanish Seas

- The model was effective at different examined locations: *MRAE* ~ 0.18, *MAE* ~ 0.18 m *bias* -0.064 m - 0.049 m, *RMSE* 0.226 m - 0.289 m (the overall highest in Begur).

Locations with high wave power

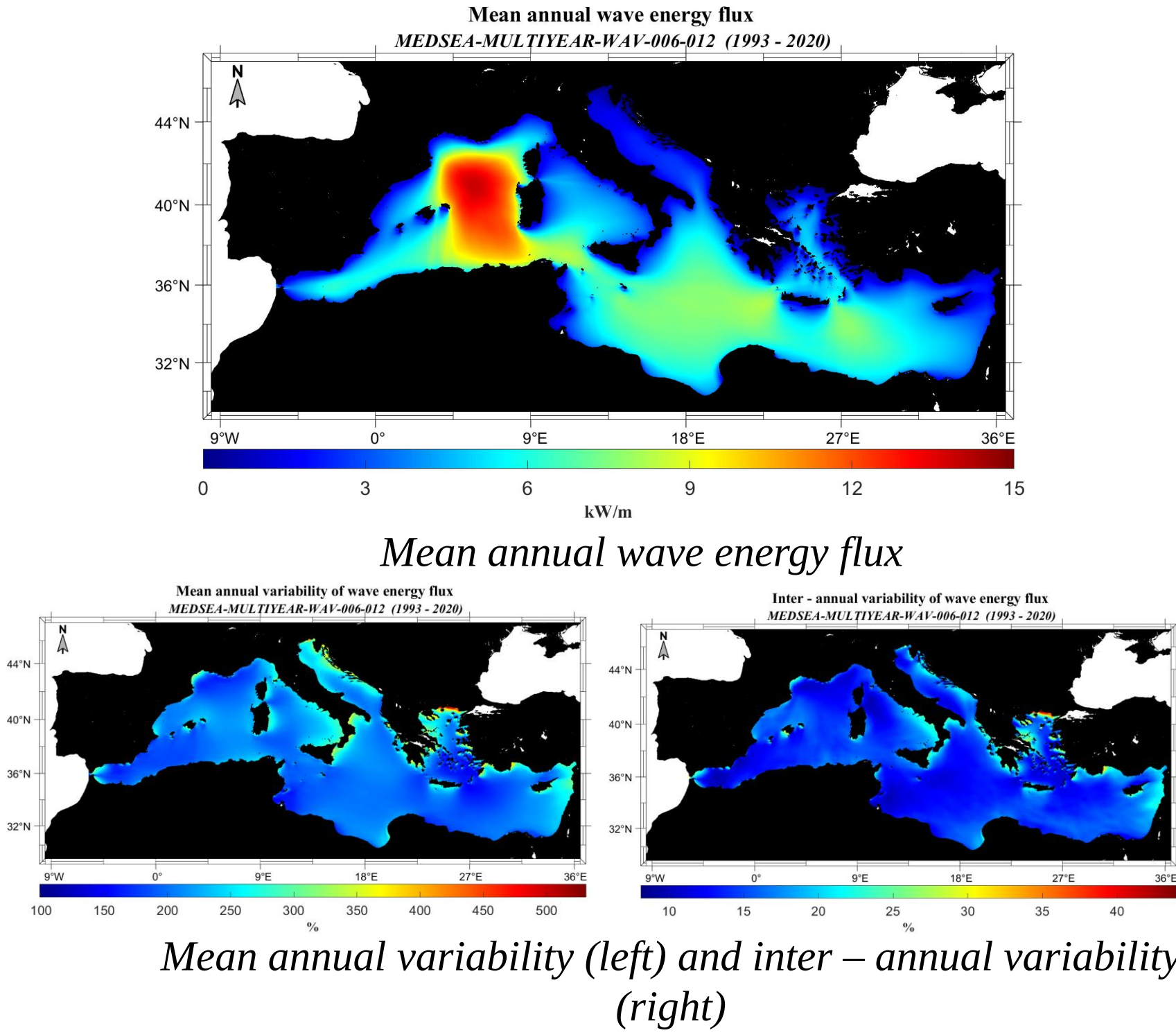
Criteria: 1) high values of mean annual wave power density;

- 2) low seasonal variability; 3) a relative shallow water depth (maximum depth of 100 m) combined with a short distance from the coast

Potential locations for WEC development

Location	Mean values of wave power (kW/m)					Prevailing directions
	AN	W	SP	SU	A	
Menorca	9.31	15	8	5	10	0°-15°
Alghero	11.03	18	10	5	11	295°-315°
Annaba	7.75	14	6	3	8	300°-345°

Wave energy flux – annual scale



Annual Slopes

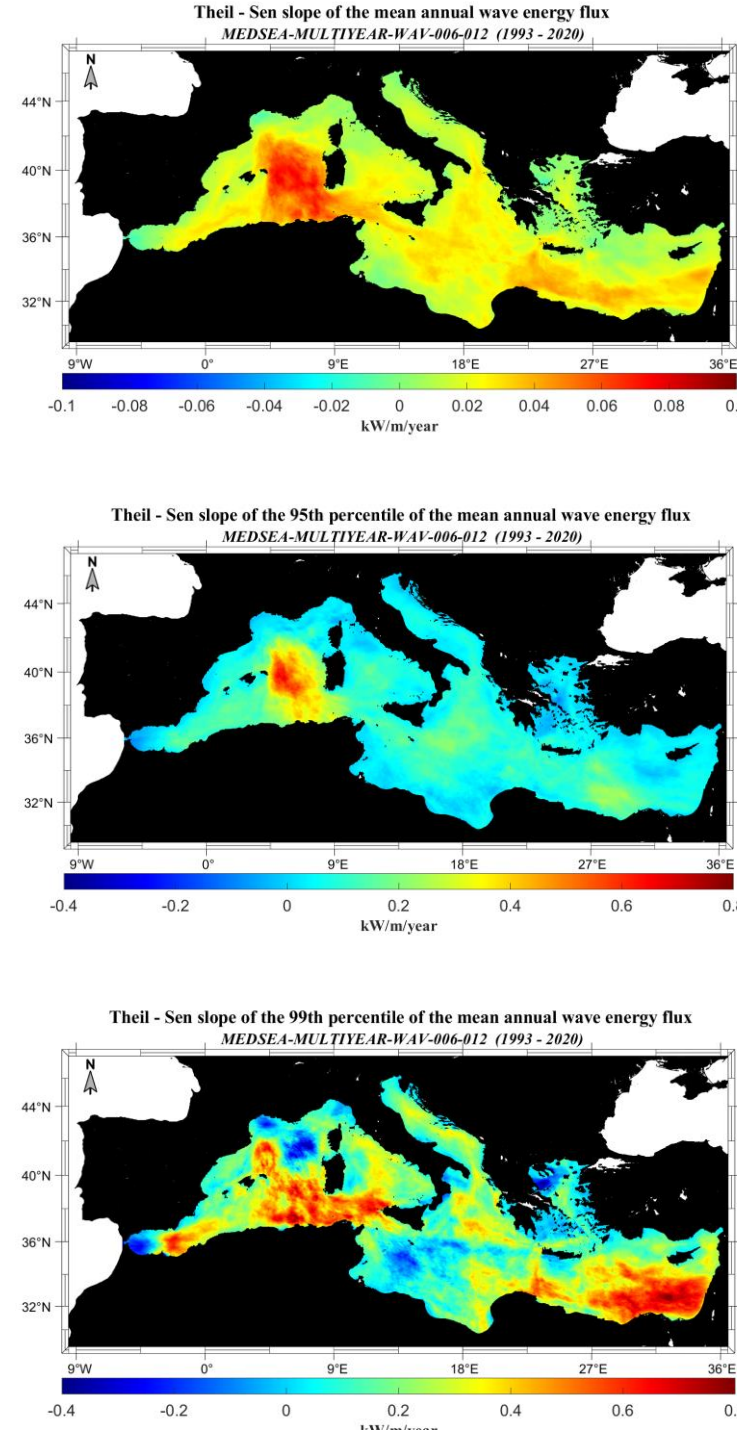
Increasing trend:

~ 0.07 kW/m/year, Gulf of Lyon, Sardinia Isl. and the coasts of Algeria.

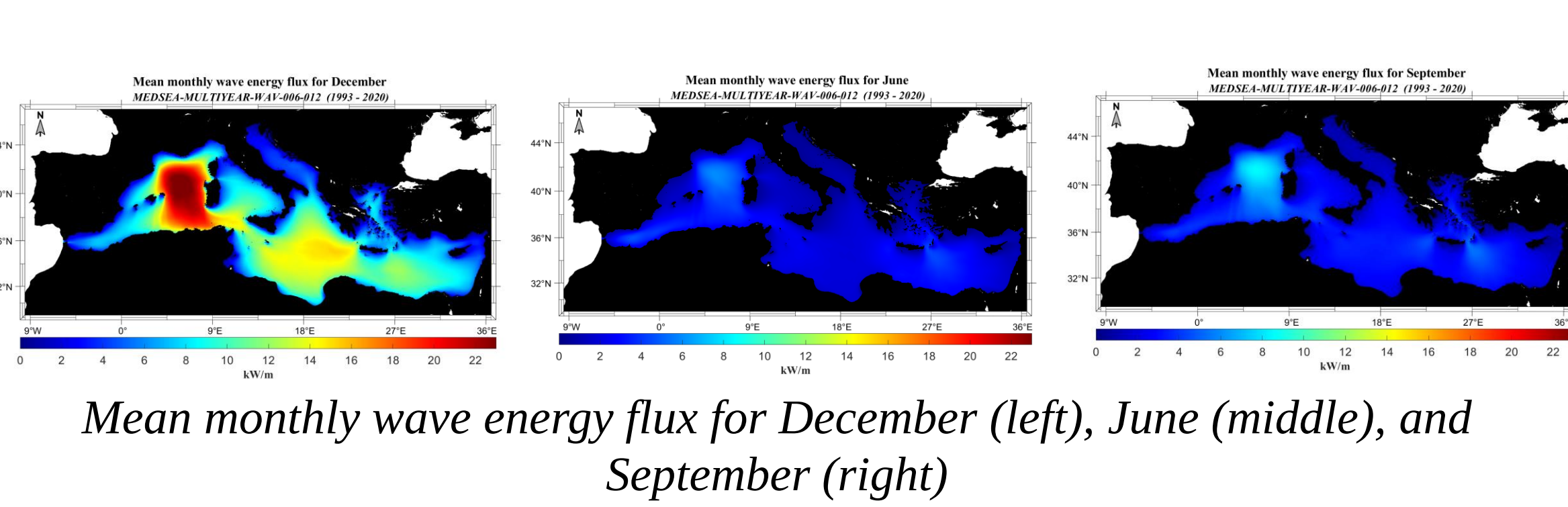
Increasing trend for the extremes:

~ 0.2 kW/m/year, Several areas of the Mediterranean Sea (especially at the SE part of the basin).

Slopes of the mean annual wave energy flux (upper), the 95 (middle) and the 99 (lower) annual percentiles

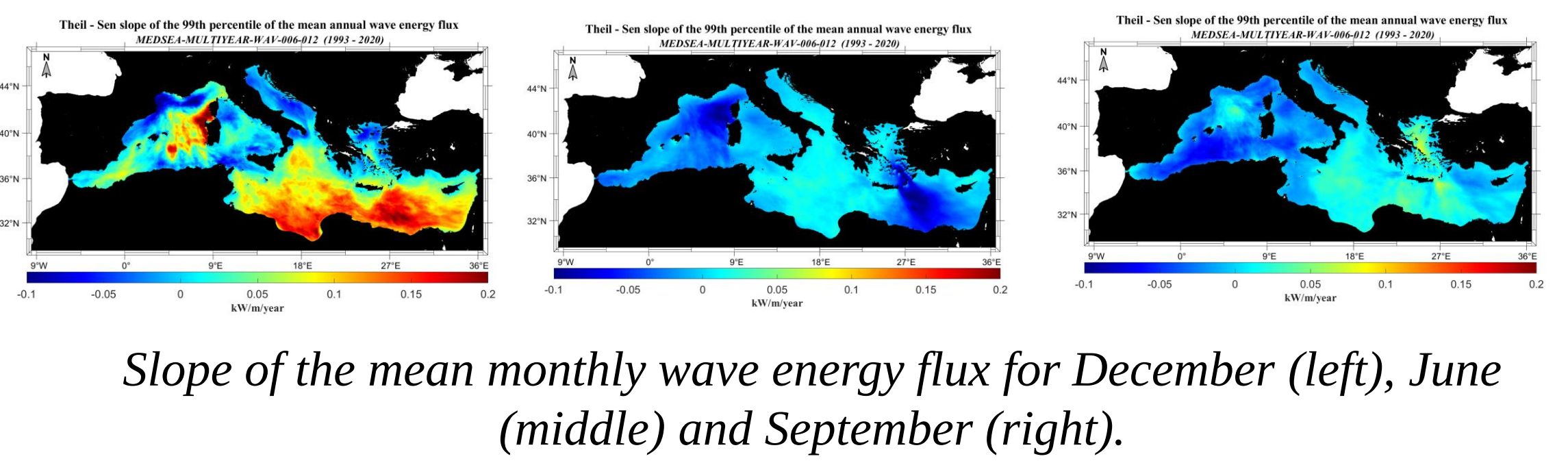


Wave energy flux – monthly scale



- The highest values have been observed during winter:** ~ 22 kW/m, at the Gulf of Lyon and African coasts
- The lowest values have been observed during June:** ~ 17 kW/m, only in the above-mentioned area and in the strait between Crete and Karpathos Isl. in the Aegean Sea

Monthly slopes



- June:** Slightly increasing trend (~0.05 kW/m/year for the central Mediterranean Sea), decreasing (for the western and south eastern Mediterranean Sea).
- September:** Increasing trend in the Aegean Sea (~0.07 kW/m/year) and a decreasing trend in western Mediterranean Sea.
- December:** Important increasing trend ~ 0.25 kW/m/year W. coasts of Sardinia Isl. and offshore areas between Crete Isl. and the coasts of Egypt.

Conclusions

- Local winds significantly affect the wave energy flux in certain areas such as the Gulf of Lyon (Mistral) and the Aegean Sea.
- The highest wave power values have been observed in the area extending from the Gulf of Lyon to SW Sardinia Isl. through the Balearic Sea up to the coasts of Algeria.
- Alghero is characterized by the highest wave resource, while similar seasonal patterns characterize all three areas.
- The variability was generally more pronounced during winter and autumn.
- With new and scaled devices, the three examined areas (Menorca Isl., Alghero and Annaba), could potentially be suitable areas for the installation of WECs.
- The main contribution to the annual mean wave energy flux occurred during winter, reaching values up to 22 kW/m

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