Improving Profitability of the Network Distribution by protecting Power Transformers with a Current Limiting Technology Device

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Abstract. This paper presents the improvement of the profitability of the Network Distribution, when power transformers are protected only with Fault Current Limiting Technologies (FCLT). In assessing the total benefits of the Network Distributions from normal to post-fault conditions, we will compare two kinds of profitability taking in account the impact of Circuit Breakers (CBs) and FCL used separately as protection devices during the life span of power transformers. This study will be performed using MATLAB/SIMULINK as software and it was concluded that the FCL perfectly improves the profitability of the Network Distribution.

Key words
MATLAB/SIMULINK, FCL, CBs, Total benefits, Profitability.

1. Introduction

In distribution network, one of the major targets is to protect the equipments, as well as the consumers. Under normal condition, the protection devices used in the circuit to protect the different equipments should not have a big disadvantage such as power loss, the voltage drop into the network distribution. The need of customer’s power quality is very important with the aim to protect their expensive equipments. During the normal conditions in the power system, a fault current limiter as well as CBs should not appear totally in the circuit because of the voltage drop and unforeseen breaking action. Therefore, during the fault condition of the network distribution, there is power loss and when the protection device comes to secure the expensive equipments in the circuit, the level of current under post fault condition voltage obtained at the primary side should not be so high for limiting the power loss under this condition. [1], [2], [3], [4], [5].

In this paper, we have studied the comparison between two types of profitability for two network distributions of which one includes CBs as protection device of power transformers and another one includes FCL for accomplishing the same action. By evaluating the Total Benefits Costs during the normal and fault operation, also we have evaluated the lifecycle cost after the lifetime of power transformer with conventional copper. The results are presented using MATLAB/SIMULINK.

2. CBs and FCL in two different Networks Distribution as protection devices

We considered two types of Network Distributions containing each the source, the line, two power transformers to be protected and the load characterizing the utility. In Figures 1 and 2 below are presented these Networks just stated above with theirs components respectively. As said above, the first Network uses the CBs as protection device for breaking the three phase system under fault operation and the second uses the FCL for limiting the fault current under abnormal operation of the three phase system.

Figure 1: Network Distribution with CBs

The FCL used for limiting the short circuit current under fault condition is a Thyristor Controlled Series Reactor (TCSR) which is presented in Figure 3 below. The current under normal operation is expressed below by the equation 1:

\[ i_{abc} (t) = I_{max} \times [\sin(\omega t + \theta_{abc} + \eta - \phi_{abc})] \] (1)

In which

- \( \theta_{abc} \) is the source voltage angle for each phase
- \( \eta \) is the firing angle of the Thyristors
- \( \phi_{abc} \) is the total impedance angle under normal condition for each phase
For both cases, the fault considered is the 3LG fault condition. For this 3LG fault, the currents and total impedance under short circuit are respectively given by the equations (2) and (3) below:

\[ I'_{ag} = m_1 \left( \sin(\alpha + \theta_a - \phi_{abc}) + \sin(\theta_a - \phi_{abc})e^{-\alpha/2} \right) \]
\[ I'_{bg} = m_2 \left( \sin(\alpha + \theta_b - \phi_{abc}) + \sin(\theta_b - \phi_{abc})e^{-\alpha/2} \right) \]
\[ I'_{cg} = m_3 \left( \sin(\alpha + \theta_c - \phi_{abc}) + \sin(\theta_c - \phi_{abc})e^{-\alpha/2} \right) \]
\[ Z_{abc} = Z_x + \sum_{i=1}^{n} R_{abc} + \sum_{j=1}^{m} Z_{abc} \]
\[ Z_{abc} = |Z_{abc}| \angle \phi_{abc} \]

Where
\[ \alpha, \beta, \xi \] represent the ratio between resistances and inductances under short-circuit.
\[ Z_{1 (abc)} \] are all impedances from primary side of power transformers.
\[ Z_{2 (abc)} \] all impedances from secondary side referred to primary side.

3. Post-fault Condition

This part is defined by the actions realized with the previous protection equipments in the circuit under abnormal operation. We are going to express the equations below of this condition related with the impact of CBs as well as of FCL in the circuit.

Applying CBs in the circuit, we have as stated above, the equations (4) and (5):

\[ I_{ag} = I'_{ag} = K (10 \text{ Cycles}) \times I_{\text{lim}} \]
\[ I_{bg} = I'_{bg} = K (10 \text{ Cycles}) \times I_{\text{lim}} \]
\[ I_{cg} = I'_{cg} = K (10 \text{ Cycles}) \times I_{\text{lim}} \]
\[ I_{\text{lim}} = I_{ag} \times \left( 1 + 2e^{-4\pi \tau (1/3)} \right) \times 0.5 \]
\[ \Delta P_1 = 3[K(\tau) \times I_{ag}] \times \sum_{i=1}^{n} R_i \]
\[ \tau = 0.5 \text{ cycles} \]

Where
\[ I_{\text{lim}} \] is the magnitude of acceptable current.
\[ I_{ag} \] is the magnitude of fault current

Applying FCL in the circuit, we have as stated above, the equations (6), (7), and (8) below:

\[ I_{\text{lim}} = p I_{\text{ag}} \left( \sin(\alpha + \theta_a - \phi_{abc}) + \sin(\theta_a - \phi_{abc})e^{-\alpha/2} \right) \]
\[ I_{\text{lim}} = p I_{\text{ag}} \left( \sin(\alpha + \theta_b - \phi_{abc}) + \sin(\theta_b - \phi_{abc})e^{-\alpha/2} \right) \]
\[ I_{\text{lim}} = p I_{\text{ag}} \left( \sin(\alpha + \theta_c - \phi_{abc}) + \sin(\theta_c - \phi_{abc})e^{-\alpha/2} \right) \]
\[ L_{FCL} = \frac{V_{FCL}}{I_{ag} \times (m - p)} \]
\[ \Delta P_2 = 3[I_{ag} \times (1 - p)] \times \sum_{i=1}^{n} R_i \]

Where
\[ p \] is the number of times the rated current
\[ V_{FCL} \] the voltage across the FCL
\[ \Delta t \] is the short circuit time

4. Profitability of the Network Distribution

This step of study is characterized by two major parts especially the normal and the fault time of the Network Distribution. For our clearance, we will evaluate both the power loss by both two types of protection devices CBs and FCL separately which will define the Life span of the power transformers.

A. Profit with the use of CBs

The Total Capital invested of the Network Distribution is defined in this case by the equation (9) below [6], [9], [10], [11]:

\[ C_T = \sum_{i=1}^{n} C_{eq} = C_G + C_T + C_{CBS} + C_{line} + C_{Me} \]

Where
\[ C_G \] is the capital invest of all equipments
\[ C_T \] is the cost of the Generator
\[ C_{CBS} \] is the cost of power transformers to protect
\[ C_{line} \] is the cost of the power cable of connection
\[ C_{Me} \] is the cost of replacements and maintenance
\[ C_{prof} \] is the Profitability of the Network after n years

The ratio between the times of fault condition and of normal condition is 0.1 and it can be expressed in term of annual time. Taking in account the cost of electricity and the lifetime of three phase power transformers, the equation (10) defines the Lifecycle Cost for this case.

\[ T_{c_{loss1}} = \Delta E_1 \times C_{KW} \times \frac{(1 + r)^{n} - 1}{r \times (1 + r)^{n}} \]

\[ T_{c_{loss2}} \] = the total amount of Power Dissipation expressed in dollars ($).

From the equation (10), we can deduce the annual energy in term of time.
\[ \Delta E_1 = \Delta P_1 \times 876 = \text{the value of Power loss after one year expressed in KWhr.} \]
C equal to the cost per kWh considered actually at \( C_{kW} = 0.05 \) $ / kWh. The capital cost for the lifecycle cost, generally \( r = 3\% \) [7, 8], and \( n \) is the number of years, or the lifetime of power transformers which generally considered equal to 25 years [12], [13].

**B. Profit with the use of FCL**

Applying the FCL in the circuit as protection device of power transformer, the Total Capital invests of the Network Distribution is defined in this case by the equation below (11):

\[
C_{eq} = C_G + C_T + C_{FCL} + C_{line} + C_{Mce} \tag{11}
\]

Where

- \( C_{FCL} \) is the investment cost of Fault Current Limiter FCL

Referring to the equation (10) above, the equation (12) below represents the LCC of the power loss related with application of Fault Current Limiter in the circuit under fault condition

\[
T_{\text{Loss}} = \Delta E_2 \times C_{kW} \times \frac{(1 + r)^n - 1}{r \times (1 + r)^n} \tag{12}
\]

The total actualised benefits of the Network Distribution during the life span of power transformer to protect is expressed as the difference between the actualised Capital investment and Benefits after 25 years considered as lifetime of power transformers. Related with what told above, the equations (13), (14) and (15) define the Profitability of the Network Distribution.

\[
C_{act, C} = C \times (1 + r)^n \tag{13}
\]

\[
B_{act} = P_{kW} \times 8760 \times C_{kW} \times \left[ \sum_{n=1}^{25} (1 + r)^n \right] \tag{14}
\]

\[
C_{Prof} = B_{act} - C_{1, act} \tag{15}
\]

Where

- \( C_{act, C} \) is the actualised capital investment after \( n \) years
- \( B_{act} \) is the actualised benefits after \( n \) years

### 5. Results of the Study

For getting the confirmation of this study, we simulated a system constituted by the source, transmission lines, two three phase power transformers to protect, and a balanced load.

**A. Data**

Two three phase power transformers (Yyn):

- 250 MVA, 300 KV, \( Z_{eq(T1)} = 5 \)
- 250 MVA, 132 KV, \( Z_{eq(T2)} = 14.62 \)
- \( C_T = 149 \) $ 368, 842 $

Source characteristics per phase:

\[
V = 10.3923 \text{KV}, H = 3 \text{x}, X_y = 1.7199, X_q = 0.23
\]

\[
T_{awr} = 0.029, X_y = 1.6598, X_q = 0.29, T_{qawr} = 0.034
\]

\[
P = 55 \text{MW}, Q = 9.03 \text{MVAR}, C_0 = 275 \times 10^6 $
\]

Transmission lines primary and secondary sides for each phase:

\[
L_a = 3 \text{mH/km}, R_a = 0.15 \Omega/km, Lengh = 80 \text{km}
\]

\[
C_{line} = 8 \times 10^6 $\]

AC Controller and Circuit Breakers: same value

\[
R_{en} = 0.001 \Omega, \eta = 90\%, m = 34, p = 2
\]

\[
C_{CBs} = 2 \times 10^5 $, \quad C_{FCL} = 25,000 $
\]

Cost of maintenance and yearly exploitation

\[
C_{act, Mce} = C_{Mce} \times \left[ \sum_{n=1}^{25} (1 + r)^n \right]
\]

The balanced Load characterized by:

\[
P = 60 \text{MW}, Q = 20 \text{MVAR}, f = 50 \text{Hz}
\]

**B. Explanation of Results**

Applying from equations1 to 8, the current’s magnitude of normal, fault and post-fault conditions and are expressed below:

**Node 1:** \( I_{abc} = 2.5 \text{KA} \), **Node 2:** \( I_{abc} = 0.36 \text{KA} \)

**Node 3** \( I_{abc} = 0.151 \text{KA} \)

**Node 1:** \( I_{abc} = 85 \text{KA} \), **Node 2:** \( I_{abc} = 12.2 \text{KA} \)

**Node 3** \( I_{abc} = 5.2 \text{KA} \)

Post-fault current with FCL after \( 1/2 \) cycles

**Node 1:** \( I_{abc} = 5 \text{KA} \), **Node 2:** \( I_{abc} = 0.72 \text{KA} \)

**Node 3** \( I_{abc} = 0.302 \text{KA} \), \( L_{FCL} = 0.05 \text{H} \)

Post-fault Currents with CBs after \( 1/2 \) cycles

**Node 1:** \( I_{abc} = 60.5 \text{KA} \), **Node 2:** \( I_{abc} = 8.68 \text{KA} \)

**Node 3** \( I_{abc} = 3.7 \text{KA} \)

Applying equations 10 and 11, the lifecycle cost related with the CBs and FCL in the Network Distribution is defined by the table 1 below and presented in Figure 4, 5 and 6.

**Table 1. Lifecycle Cost (CBs & FCL)**

<table>
<thead>
<tr>
<th>( n ) (years)</th>
<th>( T_{CT} ) (10^6 $) CBs</th>
<th>( T_{CT} ) (10^6 $) FCL</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>1835.53</td>
<td>31.96</td>
</tr>
<tr>
<td>5</td>
<td>4392.22</td>
<td>76.49</td>
</tr>
<tr>
<td>8</td>
<td>6732.2</td>
<td>117.234</td>
</tr>
<tr>
<td>10</td>
<td>8180.27</td>
<td>142.45</td>
</tr>
<tr>
<td>12</td>
<td>9542.05</td>
<td>166.17</td>
</tr>
<tr>
<td>17</td>
<td>12630.03</td>
<td>219.94</td>
</tr>
<tr>
<td>20</td>
<td>14269.92</td>
<td>248.498</td>
</tr>
<tr>
<td>25</td>
<td>16699.1</td>
<td>290.8</td>
</tr>
</tbody>
</table>

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Applying both costs and equations 13, 14 and 15, we have the results as follow in the Table 2 below which are presented in Figure 7, 8 and 9.

Table 2: Profitability of Network Distribution with the use of CB, FCL

<table>
<thead>
<tr>
<th>years</th>
<th>( C_{\omega,cb} ) [10 ^ 6$]</th>
<th>( C_{\omega,rcc} ) [10 ^ 6$]</th>
<th>( Pr_{f,cb} ) [10 ^ 5$]</th>
<th>( Pr_{rcc} ) [10 ^ 5$]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1.9</td>
<td>1.886</td>
<td>-1.617</td>
<td>-1.616</td>
</tr>
<tr>
<td>2</td>
<td>1.94</td>
<td>1.89</td>
<td>-1.395</td>
<td>-1.341</td>
</tr>
<tr>
<td>3</td>
<td>2.002</td>
<td>2.001</td>
<td>-1.166</td>
<td>1.165</td>
</tr>
<tr>
<td>4</td>
<td>2.1</td>
<td>2.06</td>
<td>-0.930</td>
<td>-0.929</td>
</tr>
<tr>
<td>5</td>
<td>2.12</td>
<td>2.12</td>
<td>-0.687</td>
<td>-0.687</td>
</tr>
<tr>
<td>6</td>
<td>2.19</td>
<td>2.18</td>
<td>-0.437</td>
<td>-0.436</td>
</tr>
<tr>
<td>7</td>
<td>2.3</td>
<td>2.25</td>
<td>-0.180</td>
<td>-0.179</td>
</tr>
<tr>
<td>8</td>
<td>2.32</td>
<td>2.3</td>
<td>0.084</td>
<td>0.086</td>
</tr>
<tr>
<td>12</td>
<td>2.613</td>
<td>2.611</td>
<td>0.885</td>
<td>0.821</td>
</tr>
<tr>
<td>17</td>
<td>3.03</td>
<td>3.02</td>
<td>2.517</td>
<td>2.519</td>
</tr>
<tr>
<td>20</td>
<td>3.31</td>
<td>3.308</td>
<td>5.873</td>
<td>5.875</td>
</tr>
<tr>
<td>25</td>
<td>3.84</td>
<td>3.335</td>
<td>7.942</td>
<td>8.441</td>
</tr>
</tbody>
</table>

For the same fault condition, the Figure 10 gives the variability of active power. When FCL applied we have Figure 11 and when CBs applied in the circuit under fault we have Figure 12 which shows that the power under post fault condition is higher.

Figure 4: Lifecycle Cost with CB in use

Figure 5: Lifecycle Cost with FCL in use

Figure 6: Comparison of LCC of CBs and FCL

Figure 7: Profit of Network with use of CBs

Figure 8: Profit of Network with use of FCL

Figure 9: Comparison of CBs and FCL’s Profits
6. Conclusion

During this study, we observed that there is a difference between protection devices such as CBs and FCL. About the Lifecycle Cost, a Network Distribution with CBs in use will get a high LCC because of the CB’s Cost of replacement, their short lifetime and the high power loss caused by their presence in the circuit. Therefore, one FCL has a less Cost and it can be used where four CBs are needed during all the life span of power transformers. The comparison related with the Profitability, a Network Distribution with FCL in use will get a high profit with the same active power required to be delivered to customer side. For companies in charge of Electrical Distribution, the use of FCL as protection devices is very perfect because of the less LCC and high profit.

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References

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